# **Two Polarization Equalization for Channel Interference Suppression**

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## INTRODUCTION

## The purpose

obtain research results toward effective methods for combating the deleterious effects of various impairments arising in digital data transmission over dually polarized communication channels

### The Problem

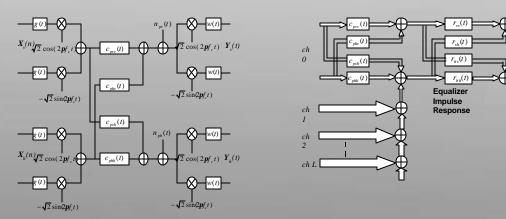
- •Co-Channel Interference (CCI)
- Adjacent-Channel Interference (ACI)
- •Cross-Polarization Interference (CPI)

## The Solution

Explore a new design possibility using:

- •Channel equalization
- •Wide receiver and transmitter bandwidth
- Derive a mathematical solution
- •Conditions and limitations

## SYSTEM MODEL



**PASSBAND and BASEBAND SYSTEM MODEL** 

**Channel Impulse Response Matrix:** 

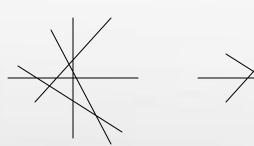
 $C(f) = \begin{bmatrix} c_{bvv}(f) & c_{bvh}(f) \\ c_{bhv}(f) & c_{bhh}(f) \end{bmatrix} \qquad R(f) = \begin{bmatrix} r_{vv}(f) & r_{vh}(f) \\ r_{hv}(f) & r_{hh}(f) \end{bmatrix}$ 

**Equalizer Impulse Response Matrix:** 

## **Finding the Receiver Impulse Response**

**Combined Channel Impulse Response:** 

$$H(f) = C(f)R(f)$$



Case One: The number of equations is greater than the number of unknowns, there is no solution

Case Two: The number of equations is less or equal to the number of unknowns, there will be at least one solution

the following conditions must be true:

 $\frac{1}{T}\sum_{k=-\infty}^{+\infty} H_0(f + \frac{k}{T}) = I \qquad \frac{1}{T}\sum_{k=-\infty}^{+\infty} H_1(f + \frac{k}{T}) = 0$ 

Suppose the receiver is band limited  $\frac{-l}{2T} < f < \frac{l}{2T}$ 

•There are two ACI channels, ch1 and ch2 •They produce eight equations •Plus four more equations by the desired channel •Thus total number of equations is 12

From frequency domain analysis •The total number of unknowns is 12 •Thus a unique solution exits

Repeat the analysis based on above method, we will find the area where the solution exists

## The Results

### Nar: number of ACI signals

 $N_{ar} = \begin{cases} 2 int(\frac{B_{i} + B_{i}}{c_{i}}), c_{i} \neq 0, c_{i} < 2B_{i} \\ 0, c_{i} \neq 0, c_{i} \geq 2B_{i} \end{cases}$ 

**Bt: relative transmitter** bandwidth

Ct: relative carrier spacing

### **NE: number of equations**

 $N_{F} = 4 (1 + N_{T})$ 

### Bri takes the values as the following:

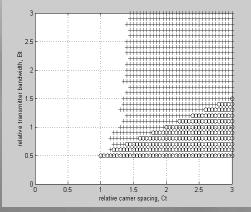
 $B_{ri} = \left\{ \frac{1}{2}, \frac{2}{2}, \frac{3}{2}, \dots, \frac{int(-2B_{r})}{2} \right\}$ 

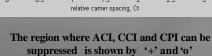
### Nu: number of unknowns

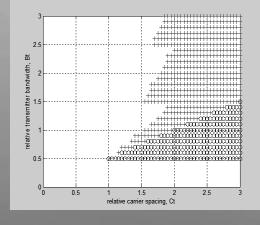
$$N_{u} = \begin{cases} 0, 2B_{t} < 1 \\ 8B_{i}, 2B_{i} \ge 1, c_{i} < 2B_{i} \\ 4[int(2\min(B_{i}; B_{i})) + 1], 2B_{i} \ge 1, c_{i} \le 2B \end{cases}$$

When  $B_r = B_t$ , the region where the Equalizer can suppress ACI, CCI and CPI is shown below:

When  $B_r = 2B_t$ , the region where the Equalizer can suppress ACI, CCI and **CPI** is shown below:







The region where ACI, CCI and CPI can be suppressed is shown by '+' and 'o'